



## UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

| CANDIDATE<br>NAME |  |  |                     |  |  |
|-------------------|--|--|---------------------|--|--|
| CENTRE<br>NUMBER  |  |  | CANDIDATE<br>NUMBER |  |  |

0580/33 **MATHEMATICS** 

Paper 3 (Core) May/June 2011

2 hours

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

Geometrical instruments Mathematical tables (optional) Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 104.



1

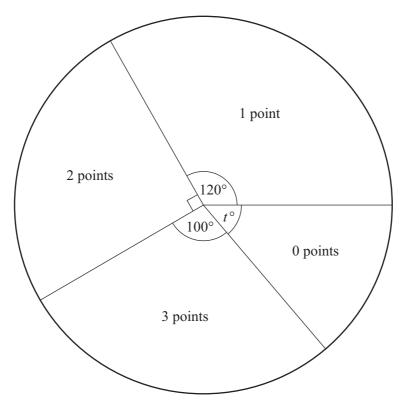
| At a theatre, adult tickets cost \$5 each and                                   | d child tickets cost \$3 each.   |
|---|--|
| (a) Find the total cost of 110 adult ticket                                     | ts and 85 child tickets.   |
|   |  |
|   | Answer(a)  [2]   |
| <b>(b)</b> The total cost of some tickets is \$750 There are 120 adult tickets. | ).   |
| Work out the number of child tickets  | 3.   |
|   | 4  |
|   | $Answer(b) \qquad [2]$   |
| (c) The ratio of the <b>number</b> of adults to                                 | the <b>number</b> of children during one performance is                              |
| a   | dults : children = 3 : 2.  |
| (i) The total number of adults and of   | children in the theatre is 150.  |
| Find the number of adults in the  | e theatre.   |
|   |  |
|   | $Answer(c)(i) \qquad [2]$  |
| (ii) For this performance, find the range Give your answer in its simplest      | atio <b>total cost</b> of adult tickets: <b>total cost</b> of child tickets. t form. |
|   |  |
|   |  |
|   | Answer(c)(ii) : [3]  |
| (d) The \$5 cost of an adult ticket is incre                                    | eased by 30%.  |
| Calculate the new cost of an adult tic  | eket.  |
|   |  |
|   | Answer(d) \$[2]  |
|   | 121377-0 (0) 4   |
| (e) The cost of a child ticket is reduced to                                    | from \$3 to \$2.70.  |
| Calculate the percentage decrease in  | the cost of a child ticket.  |
|   |  |
|   |  |
|   | Answer(e) % [3]  |

|     | P  | $\overline{Q}$ |
|-----|--|----------------|
|     |  |                |
| (a) | In the space above, construct triangle $PQR$ with $QR = 9$ cm and $PR = 7$ cm. |                |
| ()  | Leave in your construction arcs.  The line $PQ$ is already drawn.              |                |
|     | The fine T Q is already drawn.   | [2]            |
| (b) | Using a straight edge and compasses only, construct                            |                |
|     | (i) the perpendicular bisector of $PR$ ,                                       | [2]            |
|     | (ii) the bisector of angle <i>QPR</i> .  | [2]            |
|     |  | [-1            |
| (c) | Shade the region inside the triangle <i>PQR</i> which is                       |                |
|     | nearer to $P$ than to $R$ and nearer to $PQ$ than to $PR$ .                    | [1]            |
|     |  |                |
| (d) | Triangle <i>PQR</i> is a scale drawing with a scale 1 : 50 000.                |                |
|     | Find the <b>actual</b> distance $QR$ .   |                |
|     | Give your answer in kilometres.  |                |
|     |  |                |
|     |  |                |

km [2]

3 288 students took part in a quiz.
There were three questions in the quiz.
Each correct answer scored 1 point.
The pie chart shows the results.

For Examiner's Use



(a) Find the value of t.

$$Answer(a) t =$$
 [1]

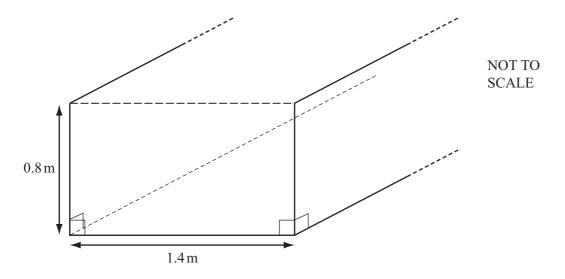
**(b)** Find the number of students who scored 2 points.

(c) Find the modal number of points.

| ( <b>a) (1)</b> Us   | se the information in the pie  | chart to cc | implete the frequ | ency table | for the 200 studen | ıs. |
|----------------------|--------------------------------|-------------|-------------------|------------|--------------------|-----|
|                      | Number of points               | 0           | 1                 | 2          | 3                  |     |
|                      | Number of students             |             |                   |            |                    |     |
| (ii) Ca              | llculate the mean number of    | points.     |                   |            |                    |     |
| ( <b>e</b> ) One stu | ident is chosen at random.     |             | Answer(d)(ii)     | ) <u></u>  |                    | [   |
| ` '                  | e probability that this studer | nt scored   |                   |            |                    |     |
|                      | points,                        |             |                   |            |                    |     |
| (ii) at              | least 1 point,                 |             | Answer(e)(i)      |            |                    | [   |
| (iii) mo             | ore than 3 points.             |             | Answer(e)(ii)     |            |                    | I   |
|                      |                                |             | Answer(e)(iii)    | )          |                    | [   |
| <b>(f)</b> 1440 st   | udents took part in the same   | quiz.       |                   |            |                    |     |
| How m                | any students would be expe     | cted to sco | ore 3 points?     |            |                    |     |
|                      |                                |             |                   |            |                    |     |
|                      |                                |             | Answer(f)         |            |                    | [   |

4

For Examiner's Use



The diagram shows part of a trench.

The trench is made by removing soil from the ground.

The cross-section of the trench is a rectangle.

The depth of the trench is 0.8 m and the width is 1.4 m.

(a) Calculate the area of the cross-section.

| Answer(a) | <br>$m^2$ | [2] |
|-----------|-----------|-----|
|           |           |     |

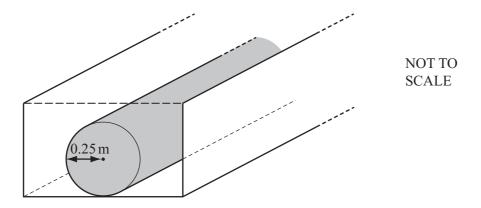
**(b)** The length of the trench is 200 m.

Calculate the volume of soil removed.

Answer(b)  $m^3$  [1]

(c)

For Examiner's Use



A pipe is put in the trench.

The pipe is a cylinder of radius 0.25 m and length 200 m.

(i) Calculate the volume of the pipe.

[The volume, V, of a cylinder of radius r and length l is  $V = \pi r^2 l$ .]

| Answer(c)(i) | <br>$m^3$ | [2] |
|--------------|-----------|-----|
|              |           |     |

(ii) The trench is then filled with soil. Find the volume of soil put back into the trench.

Answer(c)(ii) 
$$m^3$$
 [1]

(iii) The soil which is **not used** for the trench is spread evenly over a horizontal area of  $8000 \text{ m}^2$ .

Calculate the depth of this soil.

Give your answer in millimetres, correct to 1 decimal place.

Answer(c)(iii) mm [3]

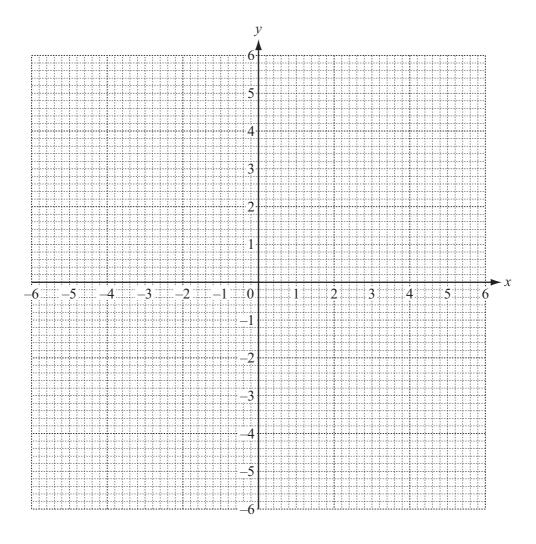
5 (a) (i) Complete the table for the function  $y = \frac{6}{x}$ ,  $x \neq 0$ .

For Examiner's Use

| х | -6 | -5   | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5   | 6 |
|---|----|------|----|----|----|----|---|---|---|---|-----|---|
| у | -1 | -1.2 |    | -2 | -3 | -6 | 6 | 3 |   |   | 1.2 | 1 |

[2]

(ii) On the grid, draw the graph of  $y = \frac{6}{x}$  for  $-6 \le x \le -1$  and  $1 \le x \le 6$ .



[4]

| х |   | -4 | -3  | -2 | -1 | 0  | 1 | 2 | 3   | 4 |
|---|---|----|-----|----|----|----|---|---|-----|---|
| J | , | 6  | 2.5 |    |    | -2 |   |   | 2.5 | 6 |

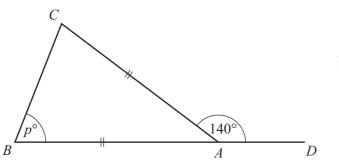
[2]

(ii) On the grid opposite, draw the graph of 
$$y = \frac{x^2}{2} - 2$$
 for  $-4 \le x \le 4$ . [4]

(c) Write down the co-ordinates of the point of intersection of the two graphs.

Answer(c)( , , , ] [2]

6 (a)



NOT TO

For

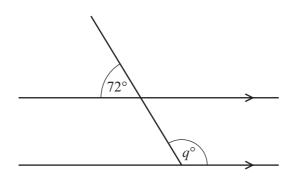
Examiner's Use

SCALE

The diagram shows a triangle ABC with BA extended to D. AB = AC and angle  $CAD = 140^{\circ}$ . Find the value of p.

Answer(a) p = [2]

**(b)** 

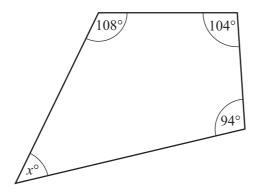


NOT TO SCALE

Find the value of q.

Answer(b) q = [2]

(c)

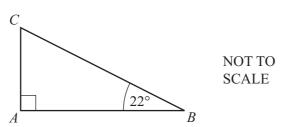


NOT TO SCALE

Find the value of x.

Answer(c) x = [1]

**(d)** 



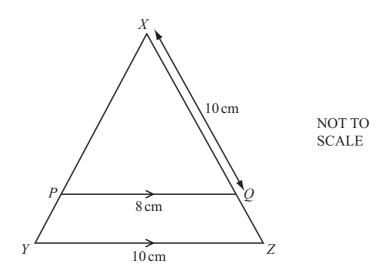
For Examiner's Use

In triangle *ABC*, angle  $A = 90^{\circ}$  and angle  $B = 22^{\circ}$ .

Calculate angle *C*.

Answer(d) Angle C = [1]

(e)



In triangle XYZ, P is a point on XY and Q is a point on XZ. PQ is parallel to YZ.

(i) Complete the statement.

Triangle *XPQ* is to triangle *XYZ*. [1]

(ii) PQ = 8 cm, XQ = 10 cm and YZ = 10 cm.

Calculate the length of XZ.

| 7   | (0) | Calria tha | agnations  |
|-----|-----|------------|------------|
| / ( | a)  | Solve me   | equations. |

(i) 
$$2x + 3 = 15 - x$$

$$Answer(a)(i) x =$$
 [2]

(ii) 
$$\frac{2y-1}{3} = 7$$

$$Answer(a)(ii) y =$$
 [2]

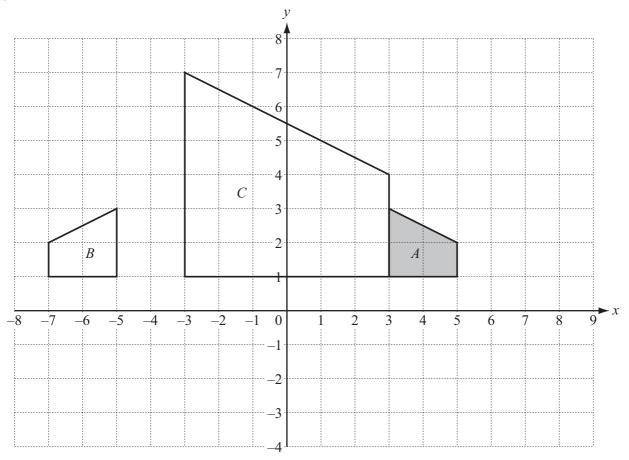
**(iii)** 
$$2 = \frac{1}{u-1}$$

$$Answer(a)(iii) u =$$
 [3]

| (b) | Write down equations to show the following.   |     |
|-----|---|-----|
|     | (i) $p$ is equal to $r$ plus two times $q$ .  |     |
|     | $Answer(b)({\rm i}) \  \   .$ (ii) $k$ is equal to the square of the sum of $l$ and $m$ .           | [1] |
|     | Answer(b)(ii)   | [2] |
| (c) | Pierre walks for 2 hours at $w \text{ km/h}$ and then for another 3 hours at $(w-1) \text{ km/h}$ . |     |
|     | The total distance of Pierre's journey is 11.5 km.  |     |
|     | Find the value of w.  |     |
|     |   |     |
|     |   |     |
|     |   |     |
|     |   |     |
|     |   |     |
|     |   |     |
|     |   |     |
|     | Answer(c) w =   | [4] |

8

For Examiner's Use



(a) On the grid, draw the images of the following transformations of shape A.

| (i) | Reflection in the <i>x</i> -axis |  | 1 |
|-----|----------------------------------|--|---|
|-----|----------------------------------|--|---|

(ii) Translation by the vector 
$$\begin{pmatrix} 3 \\ 4 \end{pmatrix}$$
 [2]

(iii) Rotation, centre 
$$(0, 0)$$
, through  $180^{\circ}$  [2]

**(b)** Describe fully the **single** transformation that maps

(i) shape A onto shape B,

(ii) shape A onto shape C.

$$Answer(b)(ii)$$
 [3]

9

•

For Examiner's Use

Diagram 1 Di

Diagram 2

Diagram 3

Diagram 4

Diagram 5

The Diagrams above form a pattern.

(a) Draw Diagram 5 in the space provided.

[1]

**(b)** The table shows the numbers of dots in some of the diagrams. Complete the table.

| Diagram        | 1 | 2 | 3 | 4 | 5 | 10 | п |
|----------------|---|---|---|---|---|----|---|
| Number of dots | 3 | 5 |   |   |   |    |   |

[5]

(c) What is the value of n when the number of dots is 737?

Answer(c) [2]

(d) Complete the table which shows the total number of dots in consecutive pairs of diagrams.

For example, the **total** number of dots in Diagram 2 and Diagram 3 is 12.

| Diagrams                   | 1 and 2 | 2 and 3 | 3 and 4 | 4 and 5 | 10 and 11 | n and $n+1$ |
|----------------------------|---------|---------|---------|---------|-----------|-------------|
| Total<br>number of<br>dots | 8       | 12      | 16      |         |           |             |

[3]

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