CANDIDATE NAME


## CENTRE

 NUMBER|  |  |  |  |  |
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CANDIDATE NUMBER


## MATHEMATICS

0580/33
Paper 3 (Core)
May/June 2011
2 hours
Candidates answer on the Question Paper.
Additional Materials: Electronic calculator Geometrical instruments
Mathematical tables (optional) Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.

Answer all questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For $\pi$, use either your calculator value or 3.142 .
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 104.

1 At a theatre, adult tickets cost $\$ 5$ each and child tickets cost $\$ 3$ each.
(a) Find the total cost of 110 adult tickets and 85 child tickets.

> Answer(a) \$
(b) The total cost of some tickets is $\$ 750$.

There are 120 adult tickets.

Work out the number of child tickets.

## Answer(b)

(c) The ratio of the number of adults to the number of children during one performance is adults : children $=3: 2$.
(i) The total number of adults and children in the theatre is 150 .

Find the number of adults in the theatre.

## Answer(c)(i)

(ii) For this performance, find the ratio total cost of adult tickets : total cost of child tickets. Give your answer in its simplest form.
Answer(c)(ii)
:
(d) The $\$ 5$ cost of an adult ticket is increased by $30 \%$.

Calculate the new cost of an adult ticket.
Answer(d) \$
(e) The cost of a child ticket is reduced from $\$ 3$ to $\$ 2.70$.

Calculate the percentage decrease in the cost of a child ticket.

## $P \longrightarrow Q$

(a) In the space above, construct triangle $P Q R$ with $Q R=9 \mathrm{~cm}$ and $P R=7 \mathrm{~cm}$.

Leave in your construction arcs.
The line $P Q$ is already drawn.
(b) Using a straight edge and compasses only, construct
(i) the perpendicular bisector of $P R$,
(ii) the bisector of angle $Q P R$.
(c) Shade the region inside the triangle $P Q R$ which is nearer to $P$ than to $R \quad$ and $\quad$ nearer to $P Q$ than to $P R$.
(d) Triangle $P Q R$ is a scale drawing with a scale $1: 50000$.

Find the actual distance $Q R$.
Give your answer in kilometres.

3288 students took part in a quiz.
There were three questions in the quiz.
Each correct answer scored 1 point.
The pie chart shows the results.

(a) Find the value of $t$.

$$
\operatorname{Answer}(a) t=
$$

(b) Find the number of students who scored 2 points.
(c) Find the modal number of points.
(d) (i) Use the information in the pie chart to complete the frequency table for the 288 students.

| Number of points | 0 | 1 | 2 | 3 |
| :---: | :--- | :--- | :--- | :--- |
| Number of students |  |  |  |  |

(ii) Calculate the mean number of points.
Answer(d)(ii)
$\qquad$
(e) One student is chosen at random.

Find the probability that this student scored
(i) 3 points,

> Answer(e)(i)
(ii) at least 1 point,
Answer(e)(ii)
(iii) more than 3 points.

## Answer(e)(iii)

(f) 1440 students took part in the same quiz.

How many students would be expected to score 3 points?


The diagram shows part of a trench.
The trench is made by removing soil from the ground.
The cross-section of the trench is a rectangle.
The depth of the trench is 0.8 m and the width is 1.4 m .
(a) Calculate the area of the cross-section.

> Answer(a)
$\qquad$ $\mathrm{m}^{2} \quad[2]$
(b) The length of the trench is 200 m .

Calculate the volume of soil removed.
(c)


$$
\begin{gathered}
\text { For } \\
\text { Examiner's } \\
\text { Use }
\end{gathered}
$$

A pipe is put in the trench.
The pipe is a cylinder of radius 0.25 m and length 200 m .
(i) Calculate the volume of the pipe.
[The volume, $V$, of a cylinder of radius $r$ and length $l$ is $V=\pi r^{2} l$.]

Answer(c)(i)
$\mathrm{m}^{3} \quad[2]$
(ii) The trench is then filled with soil.

Find the volume of soil put back into the trench.

> Answer(c)(ii)
$\qquad$ m
(iii) The soil which is not used for the trench is spread evenly over a horizontal area of $8000 \mathrm{~m}^{2}$.

Calculate the depth of this soil.
Give your answer in millimetres, correct to 1 decimal place.
$\qquad$ mm

5 (a) (i) Complete the table for the function $y=\frac{6}{x}, x \neq 0$.

| $x$ | -6 | -5 | -4 | -3 | -2 | -1 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -1 | -1.2 |  | -2 | -3 | -6 | 6 | 3 |  |  | 1.2 | 1 |

(ii) On the grid, draw the graph of $y=\frac{6}{x}$ for $-6 \leqslant x \leqslant-1$ and $1 \leqslant x \leqslant 6$.

(b) (i) Complete the table for the function $y=\frac{x^{2}}{2}-2$.

| $x$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 6 | 2.5 |  |  | -2 |  |  | 2.5 | 6 |

(ii) On the grid opposite, draw the graph of $y=\frac{x^{2}}{2}-2$ for $-4 \leqslant x \leqslant 4$.
(c) Write down the co-ordinates of the point of intersection of the two graphs.

6 (a)


$$
\begin{gathered}
\text { For } \\
\text { Examiner's } \\
\text { Use }
\end{gathered}
$$

The diagram shows a triangle $A B C$ with $B A$ extended to $D$.
$A B=A C$ and angle $C A D=140^{\circ}$.
Find the value of $p$.
(b)


## NOT TO

SCALE

Find the value of $q$.

$$
\text { Answer(b) } q=
$$

(c)


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SCALE

Find the value of $x$.
(d)


In triangle $A B C$, angle $A=90^{\circ}$ and angle $B=22^{\circ}$.
Calculate angle $C$.
(e)


In triangle $X Y Z, P$ is a point on $X Y$ and $Q$ is a point on $X Z$.
$P Q$ is parallel to $Y Z$.
(i) Complete the statement.

Triangle $X P Q$ is $\qquad$ to triangle $X Y Z$.
(ii) $P Q=8 \mathrm{~cm}, X Q=10 \mathrm{~cm}$ and $Y Z=10 \mathrm{~cm}$.

Calculate the length of $X Z$.

7 (a) Solve the equations.
(i) $2 x+3=15-x$

$$
\begin{equation*}
\text { Answer(a)(i) } x= \tag{2}
\end{equation*}
$$

(ii) $\frac{2 y-1}{3}=7$
(iii) $2=\frac{1}{u-1}$
(b) Write down equations to show the following.
(i) $p$ is equal to $r$ plus two times $q$.

Answer(b)(i)
(ii) $k$ is equal to the square of the sum of $l$ and $m$.

> Answer(b)(ii)
(c) Pierre walks for 2 hours at $w \mathrm{~km} / \mathrm{h}$ and then for another 3 hours at $(w-1) \mathrm{km} / \mathrm{h}$.

The total distance of Pierre's journey is 11.5 km .
Find the value of $w$.

8

(a) On the grid, draw the images of the following transformations of shape $\boldsymbol{A}$.
(i) Reflection in the $x$-axis
(ii) Translation by the vector $\binom{3}{4}$
(iii) Rotation, centre $(0,0)$, through $180^{\circ}$
(b) Describe fully the single transformation that maps
(i) shape $A$ onto shape $B$,

Answer(b)(i)
(ii) shape $A$ onto shape $C$.

Answer(b)(ii)

9

$\begin{array}{lllll}\text { Diagram } 1 & \text { Diagram } 2 & \text { Diagram } 3 & \text { Diagram } 4 & \text { Diagram } 5\end{array}$

The Diagrams above form a pattern.
(a) Draw Diagram 5 in the space provided.
(b) The table shows the numbers of dots in some of the diagrams.

Complete the table.

| Diagram | 1 | 2 | 3 | 4 | 5 |  | 10 |  | $n$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of dots | 3 | 5 |  |  |  |  |  |  |  |

(c) What is the value of $n$ when the number of dots is 737 ?
(d) Complete the table which shows the total number of dots in consecutive pairs of diagrams.

For example, the total number of dots in Diagram 2 and Diagram 3 is 12 .

| Diagrams | 1 and 2 | 2 and 3 | 3 and 4 | 4 and 5 |  | 10 and 11 |  | $n$ and $n+1$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total <br> number of <br> dots | 8 | 12 | 16 |  |  |  |  |  |

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